

Registration no:

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Total Number of Pages: 02

MCA
MCC504

5th Semester Regular / Back Examination 2017-18
Quantitative Techniques – II (Modelling & Simulation)

Branch:MCA

Time: 3 Hours

Max Marks: 70

Q.CODE : B708

Answer Question No.1 which is compulsory and any five from the rest.
The figures in the right hand margin indicate marks.

Q1 Answer the following questions: (2 x 10)

- a) What are the criteria to choose the constants for congruential generator of random numbers.
- b) What is the difference between mixed congruential generator and multiplicative congruential generator?
- c) If $x_0=5$ and $x_n=(3x_{n-1}+7) \bmod 10$, find x_1, x_2, \dots, x_{10} .
- d) Describe the method to generate discrete uniform random variable which take on any value $1, 2, \dots, n$.
- e) Discuss the inverse transform method to generate discrete random variables.
- f) Define stochastic process
- g) What is Markovian property?
- h) Write Chapman-Kolmogorov equations.
- i) When do the states i and j are said to be communicate?
- j) What are the different techniques to reduce variance?

Q2 a) Explain the method to generate Binomial random variable. (5)

- b) Give an efficient algorithm to simulate the value of a random variable X such that $P\{X=1\}=0.15$, $P\{X=2\}=0.3$, $P\{X=3\}=0.1$, $P\{X=4\}=0.25$ and $P\{X=5\}=0.2$ **(5)**

Q3 a) Explain the generation of standard normal random variable using polar method. (5)

- b) Describe the method to estimate π . **(5)**

Q4 (a) Use random numbers to evaluate the integral (5)

$$\int_2^5 x^2 dx$$

- (b) By using Inverse transform method generate a random variable x having distribution function $F(x)=x^n$, $0 < x < 1$ **(5)**

Q5 Write and explain the algorithm for queuing system with two servers in series. (10)

- Q6** a) Explain the use of control variates in variance reduction. **(5)**
b) Show that the variance is reduced if antithetic variables are used to estimate $\theta = E[e^U] = \int_{-1}^1 e^x dx$ **(5)**

Q7 A housewife buys three kinds of cereals: A, B and C. She never buys the same cereal on successive weeks. If she buys cereal A, then next week she buys cereal B. However if she buys either B or C, then the next week she is three times as likely to buy A as the other brand. Obtain the transition probability matrix and find out the steady state probabilities. **(10)**

- Q8** **Write Short notes on (Any TWO) :** **(5 x 2)**
- a) Acceptance rejection technique to generate discrete random variables.
 - b) Characteristics of a Markov Process.
 - c) Stratified Sampling
 - d) Importance Sampling