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Total Number of Pages: 02

**M.TECH**  
**CEPE207**

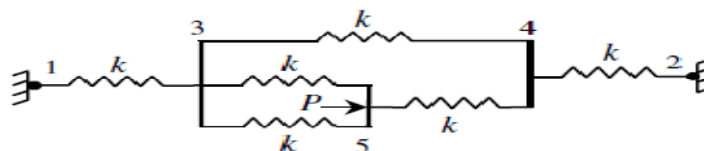
**2<sup>nd</sup> Sem Regular / Back Examination – 2015-16**  
**FINITE ELEMENT ANALYSIS OF STRUCTURES**  
**Q.CODE:W778**  
**Time: 3 Hours**  
**Max marks: 70**

**Answer Question No.1 which is compulsory and any five from the rest.**  
**The figures in the right hand margin indicate marks.**

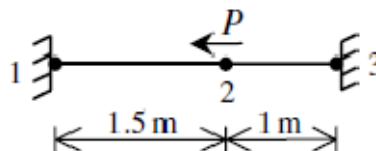
Q1 Answer the following questions: (2 x 10)

- Differentiate between essential and non-essential boundary conditions.
- Rayleigh-Ritz method has a classical form and an FE form. Comment.
- What do you mean by an admissible configuration? Explain with the help of an example.
- What is reproduction property of FEM?
- Differentiate between Cartesian and natural coordinates.
- What are isoparametric elements?
- Why convergence is required in FEA?
- Show the quadratic terms of Lagrange and Serendipity family from Pascal's triangle in 2D.
- Show with the help of an example, the calculation of equivalent nodal loads.
- What do you mean by  $C^1$  continuity?

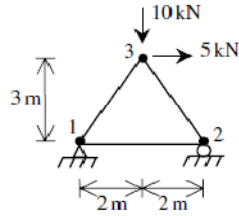
- Q2 a) Consider the spring system composed of six springs as shown in figure. Given  $k = 120 \text{ kN/m}$ ,  $P = 20 \text{ kN}$ . Determine the global stiffness matrix for the system and apply the boundary conditions. (5)



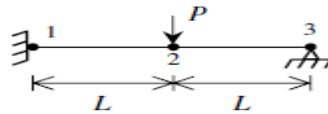
- b) Consider the structure composed of two linear bars as shown in figure. Given  $E = 210 \text{ GPa}$ ,  $A = 0.003 \text{ m}^2$ ,  $P = 10 \text{ kN}$ , and node 3 is displaced to the right by  $0.002 \text{ m}$ , determine the global stiffness matrix and get the reduced stiffness matrix. (5)



- Q3 Consider the plane truss shown.  $E = 210 \text{ GPa}$ ,  $A = 1 \times 10^{-4} \text{ m}^2$ . Assemble the structure stiffness matrix and get the reduced stiffness matrix. Also calculate the horizontal displacement at node 2. (10)



- Q4 For the beam shown in figure, the given values are,  $E = 210 \text{ GPa}$ ,  $I = 60 \times 10^{-6} \text{ m}^4$ ,  $P = 20 \text{ kN}$ ,  $L = 2 \text{ m}$ . Determine the structure stiffness matrix and vertical displacement at node 2. (10)



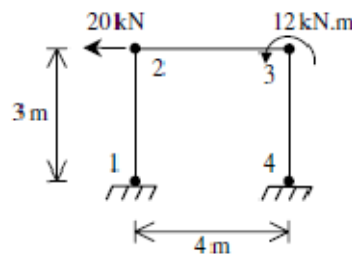
- Q5 a) Calculate the shape functions for a rectangular element having 8 nodes in natural coordinate system. (7)

- b) What is the role of shape functions in FEA? (3)

- Q6 a) Evaluate the integral  $I = \int_{-1}^1 (4^r - r) dr$  using one, two and three point Gaussian quadrature. (5)

- b) Discuss Convergence requirements in FEA. (5)

- Q7 Consider the plane frame shown in figure. Given values are,  $E = 210 \text{ GPa}$ ,  $I = 5 \times 10^{-5} \text{ m}^4$ . Assemble the global stiffness matrix of the structure. Neglect axial deformations. (10)



- Q8 (5 x 2)
- Static condensation
  - Pascal's triangle in 2D
  - Jacobian matrix for transformation.
  - Gaussian quadrature technique.